

# Red Hall Primary School Calculation Guidance Policy

	Document History
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By:	SLT
	Naomi Henry
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This policy sets out the vision for the teaching of Maths Mastery at Red Hall Primary School.

It has been written by the School Council and the Maths Subject Leader.

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## Maths Mastery at Red Hall

At Red Hall we aim to teach our children how to make sense of the world around them by developing their ability to calculate, reason and solve problems. We want our children to recognise and understand relationships and patterns in numbers in the world around them. We expect Mathematics to be utilised as a tool beyond the daily Mathematics lessons and beyond the classroom.

At Red Hall, we aim to provide our children with access to high quality teaching and learning in mathematics, which is both challenging and enjoyable! We use a Mastery approach to teaching, aiming for the deepest levels of understanding. Through mathematical talk, children will develop the ability to articulate, discuss and explain their thinking. We will provide the children with the necessary resources to allow all children to access the curriculum and encourage them to use this where appropriate to explain their logic and reasoning.

We want all pupils at Red Hall to recognise the importance of Mathematics within our daily lives, and therefore strive to be successful and resilient when they are faced with mathematical challenges. To emphasise the importance of Maths in our daily lives, we offer a broad and balanced curriculum, where Mathematical concepts are implemented within other, so that children can make rich connections not only between concepts in Maths lessons alone, but across the whole of the curriculum.

All pupils are given the same opportunities within this subject, and learning is tailored and adapted day-to-day to suit the needs of individual pupils, and support them in becoming resilient mathematicians.

## What is Maths Mastery?

Mastering maths means pupils of all ages acquiring a deep, long-term, secure and adaptable understanding of the subject. The phrase 'teaching for mastery' describes the elements of classroom practice and school organisation that combine to give pupils the best chances of mastering maths. Achieving mastery means acquiring a solid enough understanding of the maths that's been taught to enable pupils to move on to more advanced material.

NCETM, 2022.

### Aims of our Maths Curriculum:

To develop pupils who exhibit a high energy state in mathematics so that they can tackle problems with resilience and curiosity.

To have the highest of expectations for the pupils in our care. Teachers believe that ALL children in their class can achieve their age related expectation. The SLT set aspirational targets that will challenge both pupils and staff.

Lessons will begin with a 'Maths Wizard' session that is fast paced and fun. This session will include elements from all aspects of the learning so far that year. It is repetition based and intended to secure skills and consolidate learning. It is inspired by the best elements of maths teaching from Singapore and Shanghai.

Lessons will be in three main parts:

- 1. Pictorial where the teacher will introduce an objective using visual representations. Teaching will begin at the stage below and then move up the age related expectation. This builds on prior learning.
- 2. Concrete teaching now moves onto the use of apparatus to help consolidate learning.
- 3. Abstract where learning will be expressed in a written form perhaps in the form of a calculation.

The national curriculum for mathematics and this numeracy policy aims to ensure that all pupils:

- become fluent in the fundamentals of mathematics, including through varied and frequent practice with increasingly complex problems over time, so that pupils have conceptual understanding and are able to recall and apply their knowledge rapidly and accurately to problems
- **reason mathematically** by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language

• can **solve problems** by applying their mathematics to a variety of routine and nonroutine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions.

## Teaching and Learning of Maths Mastery

Teachers will use the new 2014 Mathematics Curriculum as well as White Rose and Maths No Problem! resources to plan a series of lessons that will meet the needs of pupils and progress their learning in a Mastery approach.

### **Objectives and Stages**

The objectives are grouped into years – so that there is an expectation that the vast majority of, for example, Year 5 pupils will be accessing the Year 5 assessment grid.

At Red Hall, these yearly expectations have been turned into 'stages', and children work towards targets which are appropriate for the stage they are working on. The Assessment Grids give staff the opportunity to track the progress of children termly, and help to inform future planning and next steps in progression towards a deeper understanding of a concept.

#### Learning Journey

Teachers will plan using S Plan format (Appendix 1). The aim of an S Plan is to make explicit, the journey through a concept, breaking each concept into small steps which are achievable for all pupils. A differentiated sequence of learning will be created, based on the stages that the pupils in each class are currently working on. This plan will be evaluated as the children make their way through their journey of learning and appropriate intervention and support will be given to those children who need to secure some targets, having a 'keep-up' not 'catch-up' approach to intervention. Over the course of a term, teachers must ensure that a range of topics are covered, as set out in the long term planning.

#### Sequence of a Lesson

All Maths lessons will begin with a 'Maths Wizard' session, to meet the mental mathematic objectives explicit in the new curriculum and to review prior learning and to inform and scaffold new learning.

The lesson will then progress through a series of activities which require children to demonstrate their fluency skills as well as problem solving and reasoning. Please see Appendix 2 for KS1 sequence of lessons and Appendix 3 for KS2 sequence of lessons.

#### Yearly Expectations

The national expectations are that a child will be accessing the objectives pertinent to their year group. Below are the expectations for each year group, linked to the new national curriculum and our assessment policy:

Year 1 – Stage 1 – National Standard Year 2 – Stage 2 - National Standard Year 3 – Stage 3 - National Standard Year 4 – Stage 4 - National Standard Year 5 – Stage 5 - National Standard Year 6 – Stage 6 - National Standard

Children working at a 'Mastery' level are considered as having a deep level of understanding.

Please see our Assessment Policy for these assessment grids.

## Non-Negotiables for the Teaching of Maths

- 1. Children must work in pencil and use a ruler
- 2. Work must be presentable, with one number in each box
- 3. Short date always used, i.e. 1.1.2020
- 4. The short date must be underlined using a ruler
- 6. Children MUST self-assess their work at the end of every lesson, from Y2 to Y6
- 7. Opportunities for children to self-check their fluency work must be evident

8. Feedback given in blue pen linked to LO if necessary. No 'well done' but explaining how to improve (using cursive script handwriting) or challenging further

9. Green pen to be used for any misconception corrections or green pen challenges

10. Problem Solving and Reasoning work quality marked, with clear feedback to ensure misconceptions are addressed and more-able children are challenged further

11. Clear challenge given to more-able pupils, which is shown by appropriately differentiated work within fluency challenges

12. Assessment grids to be marked and kept up to date once each objective is covered and children are secure with that element of the concept

Termly scrutinies will monitor how each class is performing against these criteria.

## Calculation Guidance for the Four Operations

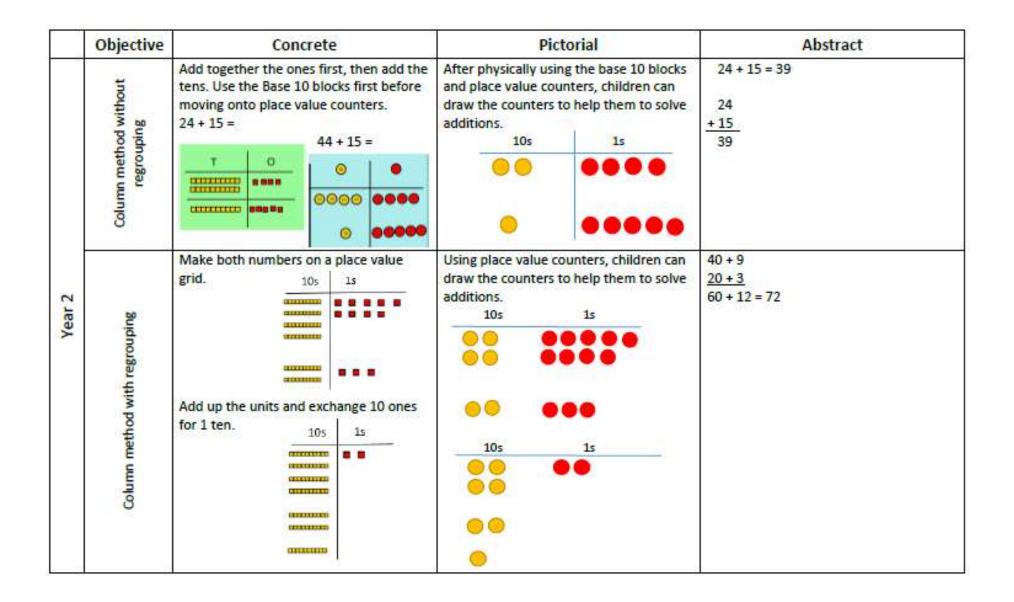
The following calculation guidance has been devised has been developed from the White Rose Calculation Policy: working document, which was written as a guide to indicate the progression through Addition, Subtraction, Multiplication and Division in Years 1 – 6. This guidance is our recommendation, in line with work completed by Maths Mastery / Sustaining Mastery / Mastering Number Maths Hub (NCETM: National Centre for Excellence in the Teaching of Maths) and White Rose Maths. Teachers can use any teaching resources that they wish to use and the policy does not recommend one set of resources over another, rather that, a variety of resources are used. For each of the four rules of number, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. The principle of the concrete-pictorial-abstract (CPA) approach [Make it, Draw it, Write it] is for children to have a true understanding of a mathematical concept, they need to master all three phases within a year group's scheme of work.





# **ADDITION**

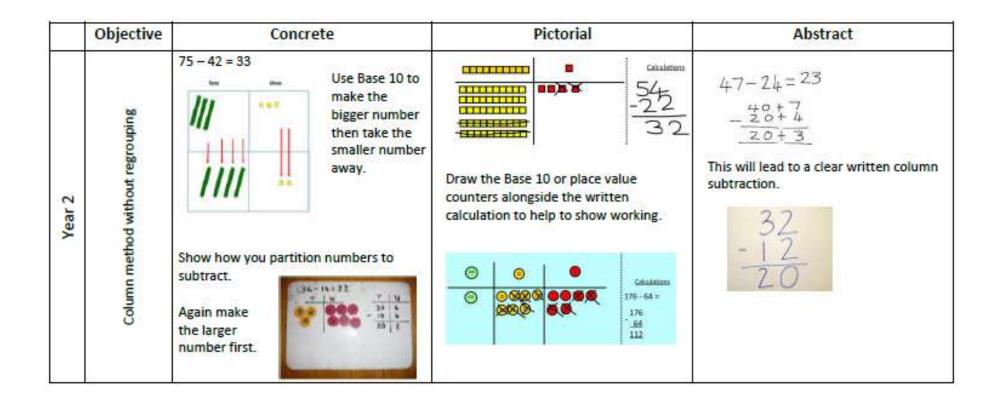
c—13	Objective	Concrete	Pictorial	Abstract
ar 1	Number bonds of 5, 6, 7, 8, 9 and 10	Use cubes to add two numbers together as a group or in a bar.	Image: state stat	2+3=5 3+2=5 5=3+2 5=2+3 Use the part-part-whole diagram as shown above to move into the abstract.
Year 1	Counting	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	Use a number line to count on in ones. 5 6 7 8	5 + 3 = 8



	Objective			Concrete	e		Pict	orial	Abstract
12		Make both numbers on a place value grid.		100s	10s	15	$   \begin{array}{r}     100 + 40 + 6 \\     500 + 20 + 7 \\     600 + 70 + 3 = 673   \end{array} $		
Year 3/4	Column method with regrouping	for 1 te	o the unit en. 0000 000 000 000 000 000 000 000 000	e on to d ce value o learning.	hange 10 ones 146 ±527 ecimals, money counters can be	represent value cou learning a NB Additi	nters to fui ind underst	e columns and place rther support their tanding. ey needs to have £	As the children progress, they will move from the expanded to the compacted method. 146 + 527 673 1 As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.
Year 5/6	Column method with regrouping	Consol	lidate uno	derstandir	ng using numbers	s with more	than 4 digi	its and extend by add	ing numbers with up to 3 decimal places.

# **SUBTRACTION**

1	Objective	Concrete	Pictorial	Abstract
	Taking away ones	Use physical objects, counters, cubes etc. to show how objects can be taken away. 4-2=2	Cross out drawn objects to show what has been taken away. 4-2=2	4 - 2 = 2
Year 1	Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number, showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
	Find the difference	Compare amounts and objects to find the difference.	+5 Count on to find the difference. Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 ? Lisa Sister 22 Draw bars to find the difference between 2 numbers.	Hannah has 8 goldfish. Helen has 3 goldfish. Find the difference between the number of goldfish the girls have.



Objective	Concrete	Pictorial	Abstract
Column method with regrouping	Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges. Make the larger number with the place value counters	2007A0507999	Children can start their formal written method by partitioning the number into clear place value columns. $\boxed{728 - 582 + 144} + \frac{5}{7} + \frac{8}{2} + \frac{8}{3} + \frac{5}{7} + \frac{2}{2} + \frac{8}{3} + \frac{5}{7} + \frac{2}{2} + \frac{8}{3} + \frac{5}{7} + \frac{2}{2} + \frac{8}{3} + \frac{5}{7} + \frac{2}{4} + \frac{8}{3} + \frac{2}{7} + \frac{8}{3} + \frac{8}{3}$

Objective	Concrete	Pictorial	Abstrac
regrouping	Now look at the tens, can I take away 8 tens easily? I need to exchange 1 hundred for 10 tens.		
Column method with regrouping	complete my subtraction.		
Colum	Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.		

# **MULTIPLICATION**

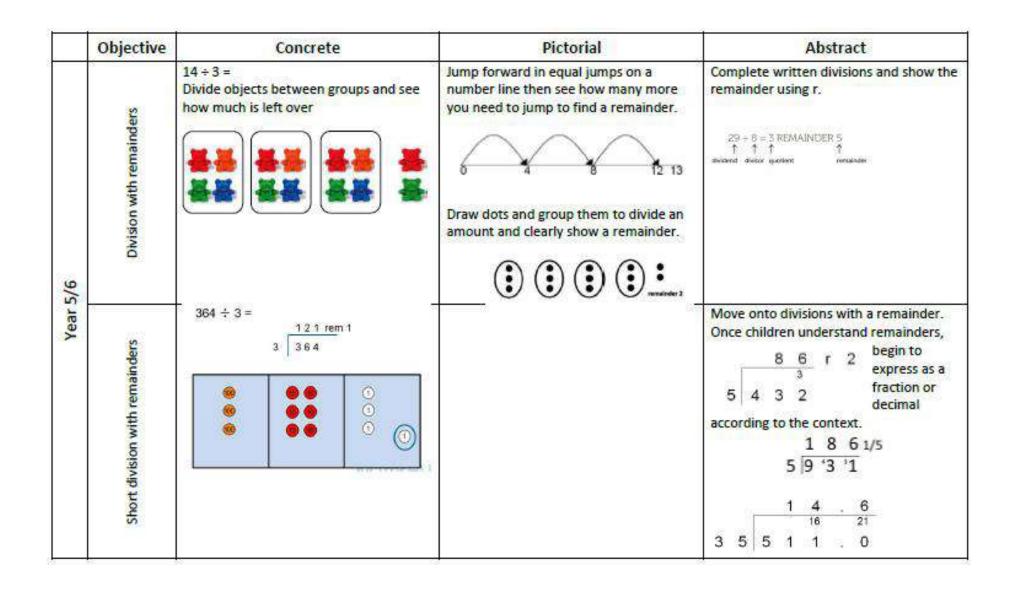
	Objective	Concrete	Pictorial	Abstract
22	Repeated addition	Use different objects to add equal groups,	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2+2+2=6 5 1 2+2+2=6 5 5 5 5 5 5 5 5	Write addition sentences to describe objects and pictures. 52 $53$ $532+2+2=6$
Year 1/2	Arrays- showing commutative multiplication	Create arrays using counters/cubes to show multiplication sentences.	Draw arrays in different rotations to find commutative multiplication sentences. $4 \times 2 = 8$ $2 \times 4 = 8$ $2 \times 4 = 8$ $4 \times 2 = 8$ $2 \times 4 = 8$ $4 \times 2 = 8$ Link arrays to area of rectangles.	Use an array to write multiplication sentences and reinforce repeated addition. 5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 $5 \times 3 = 15$ $3 \times 5 = 15$

-	Objective	Concrete	Pictorial	Abstract
Year 5/6	Compact method	Children can continue to be supported by place value counters at the stage of multiplication.	Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods. $\boxed{\begin{array}{c} \hline \\ \\ \\ \\ \\ \\ $	Start with long multiplication, reminding the children about lining up their numbers clearly in columns. If it helps, children can write out what they are solving next to their answer. 7 4 $\times$ 6 5 1 2 2 1 8 2 4 0 $\pm$ 4 2 0 0 $\pm$ 4 2 0 0 $\pm$ 4 2 0 0 $\pm$ 3 4 0 $\pm$ 4 2 0 0 $\pm$ 3 4 2 This moves to the more compact method. $\frac{x + x}{1342}$ $\frac{x + x}{18}$ 13420 10736 24156

## DIVISION

	Objective	Concrete	Pictorial	Abstract
	Sharing	I have 8 cubes, can you share them equally between two people?	Children use pictures or shapes to share quantities. $ \begin{array}{c}                                     $	Share 8 buns between two people. 8 ÷ 2 = 4
Year 1/2	Grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 +	10 ÷ 5 = 2 Divide 10 into 5 groups. How many are in each group?

	Objective	Concrete	Pictorial	Abstract
. 18	Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg 15 ÷ 3 = 5 5 x 3 = 15 15 ÷ 5 = 3 3 x 5 = 15	Draw an array and use lines to split the array into groups to make multiplication and division sentences.	Find the inverse of multiplication and division sentences by creating four linking number sentences. 5 x 3 = 15 3 x 5 = 15 15 ÷ 5 = 3 15 ÷ 3 = 5
Year 3/4	Short division	Use place value counters to divide using the short division method alongside. 96 ÷ 3 3 42 ÷ 3 Start with the biggest place value. We are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over. We exchange this ten for 10 ones and then share the ones equally among the groups. We look at how many are in each group.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups. Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder.



Ob	jective	Concrete	Pictorial	Abstract
Year 6	long division	Concrete	Pictorial	Children will use long division to divide numbers with up to 4 digits by 2 digit numbers. 015 32 487 -0 48 -32 -32 167
Yea	Long di			$     \frac{160}{7}     \frac{17}{546} r 19     31 546     \frac{311}{236}     \frac{217}{19}     $

APPENDIX 1 S Plan Example

5 Plan - Auturn 2 - Multiplication and Division True or Fals ORAL Reasoning. \* GHS } consoludate MS 2,5,10. Do yo Arrays - Really The 3x Table, the to The 4x Table, Arrays - Real life Repeated addition Counters Tavers Counters Table Troopers Arrays - Real life 7 Number SHICK Counters · Inverse means opposite Table Troopens A Number Stick troopens of adding each doncept Reinfarce 1×3 = 7 toble troopens of adding each donce 2×3 = times table facts. Table Troopens The 8x Table \* inverse bo to taught as yellow challenge. Deviding Equal ups stared Courters Uniding Hoops (practice) TTRS check gride. end, multiplication aside Not knowing Short Outside th Multiplication bus stop. Short How many Number Stick Columns equal Counters Durusion What do already, TTRS check grids with the ones groups ! Numcon as prompts Confusing with Column. Counters Culum addition Solving I-step Hoops Chalk - bus stop. Beginning in Problems 10's. Solving 2. Step RUCSAC. De you agree? . Problems. Truel De you agree? . Folse De Leplain 1 Justifies \* Resources \* \* STEM Sentences \* \* Reasoning \* \* Poss. Misconceptions \* \* Evaluate \*

# APPENDIX 2 Sequence of Lessons - KS1

Monday	Fluency	I would expect that on Monday, all children are
,,	Using equipment / visual aids to	provided with the same opportunity, so that
	develop understanding where	assumptions aren't made of their abilities, unless they
	possible.	are working significantly below the expected standard
	Begin lesson with a problem solving question	for that point in the year. On Tuesday, you may challenge more-able, based on learning from prior day.
	/ reasoning question to give a context /	I.e this could be through giving them numbers with
	purpose for learning	more digits for the four operations. This means
Tuesday	Fluency	looking at differentiating work! If you need help or
	Visual Fluency	suggestions, please ask!
	Try to encourage only SEND /	Provide the children with the answers for fluency
	children at risk of	tasks in a small box beside the questions! This way,
	underachieving targets to use	they can mark off when they have the answer right an
	resources to support learning.	if it is not in the grid, they need to have another go with a green pen! This makes marking much easier for
	Begin lesson with a problem solving question	you too, and gives you time to quality mark problem
	/ reasoning question to give a context /	solving and reasoning tasks as these are key evidence
	purpose for learning	that a child has secured a skill!
Wednesday	Fluency	Please remember what is meant by varied fluency:
	Visual Fluency	procedural or conceptual variation. Conceptual means
	Try to encourage only SEND /	visual representations to help, procedural means
	children at risk of	<ul> <li>applying learning. Example of procedural could be:</li> <li>when looking at multiplication facts: if we know 5 x 6 = 30,</li> </ul>
	underachieving targets to use	what would this be: 50 x 6 = ?
	resources to support learning.	<ul> <li>When looking at addition and subtraction:</li> </ul>
	Begin lesson with a problem solving question	12,343 + ? = 54,709
	/ reasoning question to give a context / purpose for learning	Using the inverse to write the answer or
Thursday	Fluency	finding links and connections between sums:
indi Sady	Varied Fluency	122-92 119-89
	vulled Fluency	The year and againtened with this places only mal
	Begin lesson with a problem solving	If you need assistance with this, please ask me! Please note: not all children will progress to problem
	question / reasoning question to give a	solving / reasoning activities at the same time. You
	context / purpose for learning	need to make a professional, teacher assessment as to
		who can move on and who does not. These activities
		may likely need to be differentiated from now on too,
Friday	Problem Solving / Reasoning	depending on abilities to use and apply skills. There
, riddy	r oblem contring / reasoning	should be a range of problem solving, not use word
	Applying skills taught	problems. Use true/false, missing number problems, complete the sentence. <b>Remember, these should be</b>
		quality marked too, providing clear feedback for
	Developing reasoning skills to	misconceptions and clear challenge for more-able
	demonstrate a deeper	pupils to progress.
	understanding of concepts	I understand you may spend more than one week per
		concept, which is absolutely fine. Just please stick to
	- 0	this sequencing once a new concept has been
Deor	m Believe Achieve	introduced (so you may spend 4 days on fluency or you
Gra	" Banar unice	may spend more than two days on reasoning / problem solving etc).

# APPENDIX 3 Sequence of Lessons – KS2

Monday	Fluency	I would expect that on Monday, all children are
monauy	Using equipment / visual aids to	provided with the same opportunity, so that
	develop understanding where	assumptions aren't made of their abilities, unless they
		are working significantly below the expected standard
	possible.	for that point in the year. On Tuesday, you may
	Begin lesson with a problem solving question / reasoning question to give a context /	challenge more-able, based on learning from prior day.
	purpose for learning	I.e this could be through giving them numbers with
Tuesday	Fluency	more digits for the four operations. This means looking at differentiating work! If you need help or
,	Moving to abstract.	suggestions, please ask!
	Try to encourage only SEND /	Provide the children with the answers for fluency
	children at risk of	tasks in a small box beside the questions! This way,
		they can mark off when they have the answer right an
	underachieving targets to use	if it is not in the grid, they need to have another go
	resources to support learning.	with a green pen! This makes marking much easier for
	Begin lesson with a problem solving question / reasoning question to give a context /	you too, and gives you time to quality mark problem
	purpose for learning	solving and reasoning tasks as these are key evidence
Wednesday	Fluency	that a child has secured a skill
	Varied Fluency	Please remember what is meant by varied fluency: procedural or conceptual variation. Conceptual means
		visual representations to help, procedural means
	Begin lesson with a problem solving	applying learning. Example of procedural could be:
	question / reasoning question to give a	• when looking at multiplication facts: if we know 5 x 6 = 30,
	context / purpose for learning	<ul> <li>what would this be: 50 x 6 = ?</li> <li>When looking at addition and subtraction:</li> </ul>
		12,343 + ? = 54,709 Using the inverse to write the answer
Thursday	Problem Solving / Reasoning	or
	· · · · · · · · · · · · · · · · · · ·	finding links and connections between sums:
	Applying skills taught	122-92 119-89
	Developing reasoning skills to	If you need assistance with this, please ask me!
		Please note: not all children will progress to problem
	demonstrate a deeper	solving / reasoning activities at the same time. You
	understanding of concepts	need to make a professional, teacher assessment as to
		who can move on and who does not. These activities
		may likely need to be differentiated from now on too,
		depending on abilities to use and apply skills. There
Friday	Problem Solving / Reasoning	should be a range of problem solving, not use word problems. Use true/false, missing number problems,
		complete the sentence. <b>Remember, these should be</b>
	Applying skills taught	quality marked too, providing clear feedback for
	Developing reasoning skills to	misconceptions and clear challenge for more-able
	demonstrate a deeper	pupils to progress.
	understanding of concepts	I understand you may spend more than one week per
		concept, which is absolutely fine. Just please stick to
		this sequencing once a new concept has been
ົ້າ	na Poliona Calina	introduced (so you may spend 4 days on fluency or you
Brea	m Believe Achieve	may spend more than two days on reasoning / problem
	• • • •	solving etc).